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| Carnegie Mellon Univ. |
| School of Computer Science |
| 15-415/615 - DB Applications |
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| Lecture \#4: Relational Algebra |
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## Overview

- history
- concepts
- Formal query languages
- relational algebra
- rel. tuple calculus
- rel. domain calculus

- before: records, pointers, sets etc
- introduced by E.F. Codd in 1970
- revolutionary!
- first systems: 1977-8 (System R; Ingres)
- Turing award in 1981


## Concepts - reminder

- Database: a set of relations (= tables)
- rows: tuples
- columns: attributes (or keys)
- superkey, candidate key, primary key



## Example: cont'd

- Di: the domain of the i-th attribute (eg., char(10)




## Formal query languages

- How do we collect information?
- Eg., find ssn's of people in 415
- (recall: everything is a set!)
- One solution: Rel. algebra, ie., set operators
- Q1: Which ones??
- Q2: what is a minimal set of operators?


- Anuscs




## Relational operators

- 
- 
- .
- set union U
- set difference '_'


## Other operators?

- Notice: selection (and rest of operators) expect tables, and produce tables ( $->$ can be cascaded!!)
- For selection, in general:

$$
\sigma_{\text {condition }} \quad(R E L A T I O N)
$$

| Selection - examples |  |  |
| :---: | :---: | :---: |
| - Find all 'Smiths' on 'Forbes Ave' |  |  |
| $\sigma_{\text {name='Smith' } \wedge ~ a d d r e s s=' F o r b e s ~ a v e ' ~}(S T U D E N T)$ |  |  |
| 'condition' can be any boolean combination of ' $=$ ‘, '>’, ‘>=‘, ... |  |  |
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| Relational operators |  |  |  |
| - selection | $\sigma_{\text {condition }}$ |  |  |
| - set union | R U S |  |  |
| - set difference | R-S |  |  |
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## Relational operators

Cascading: 'find ssn of students on 'forbes ave'

| $\pi_{s s n}\left(\sigma_{\text {address='f orbesave' }}(S T U D E N T)\right)$ |  |  |
| :---: | :---: | :---: |
| STUDENT |  |  |
| Ssn | Name | Address |
| 123 | smith | main str |
| 234 | jones | forbes ave |



## Relational operators

Are we done yet?
Q: Give a query we can not answer yet!


## Relational operators

A: any query across two or more tables, eg., 'find names of students in 15-415'
Q: what extra operator do we need??
A: surprisingly, cartesian product is enough!

| STUDENT |  |  |
| :--- | :--- | :--- |
| Ssn |  | Name |
|  | 123 | smith |
|  | Address |  |
| 234 | jones | forbes ave |



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| $5^{\text {cmuscs }}$ |  |  |  |  |  |
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| so what? |  |  |  |  |  |
| - Eg., how do we find names of students taking 415? |  |  |  |  |  |
| STUDENT |  | SSN | c-id | grade |  |
| Ssn Name | Address | 123 | 15-415 | A |  |
| 123 smith | main str |  | 15-413 | B |  |
| 234 jones | forbes ave |  |  |  |  |
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## Overview - rel. algebra

- fundamental operators
- derived operators
- joins etc
- rename
- division
- examples

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## Division

- Observations: ~reverse of cartesian product
- It can be derived from the 5 fundamental operators (!!)
- How?




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| Division <br> SHIPMENT |  |  |
| - Answer: | s\#  <br> $\mathbf{s 1}$ $\frac{\mathrm{p} \#}{\text { p } 1}$ | BAD_s |
|  | s2 p1 <br> S1  | $=\frac{\mathrm{st}}{\mathbf{s i n}}$ |
|  | $\begin{array}{ll}\text { s1 } & \text { p1 } \\ \mathbf{s 1} & \text { p2 } \\ \mathbf{s 3} & \text { p1 }\end{array}$ |  |
|  | s5 p3 |  |
| $r \div s=\pi_{(R-S)}(r)-\pi_{(R-S)}\left[\left(\pi_{(R-S)}(r) \times s\right)-r\right]$ |  |  |
|  |  |  |
| all possible |  |  |
| suspicious shipments |  |  |
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| Sample schema <br> find names of students that take $15-415$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| STUDENT |  |  |  | CLASS |  |  |
| Ssn | Name | Add | dress | c-id | c-name | units |
| 123 | smith | main | n str | 15-413 | s.e. | 2 |
| 234 | jones | forb | es ave | 15-412 | O.s. | 2 |
|  |  | TAKES |  |  |  |  |
|  |  | SSN | c-id | grade |  |  |
|  |  | 123 | 15-413 | A |  |  |
|  |  | 234 | 15-413 | B |  |  |
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| $3^{\text {a }}$ cuscs |  |  |
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| Examples |  |  |
| - find course names of 'smith' |  |  |
| $\pi_{c-\text { name }}\left[\sigma_{\text {name }} \operatorname{smmih}(\right.$ |  |  |
| $\xrightarrow{\text { STUDENT® } \triangle \text { TAKES } \triangle C L A S S ~}$ |  |  |
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## Examples

- find ssn of 'overworked' students, ie., that take 412, 413, 415 -Correct answer:

$$
\begin{aligned}
& \pi_{s s n}\left[\sigma_{c-\text { name }=412}(T A K E S)\right] \cap \\
& \pi_{s s n}\left[\sigma_{\text {c.name-413 }}(T A K E S)\right] \cap \\
& \pi_{\text {ssn }}\left[\sigma_{c \text { c.name-415 }}(T A K E S)\right]
\end{aligned}
$$

## Examples

- find ssn of students that work at least as hard as $\operatorname{ssn}=123$, ie., they take all the courses of ssn=123, and maybe more


## ${ }^{3}$ cuscs <br> Examples

- find ssn of students that work at least as hard as $\mathrm{ssn}=123$ (ie., they take all the courses of $\mathrm{ssn}=123$, and maybe more
$\left[\pi_{s s n, c-i d}(T A K E S)\right] \div \pi_{c-i d}\left[\sigma_{s s n=123}(T A K E S)\right]$
Conclusions
- Relational model: only tables ('relations')

| - relational algebra: powerful, minimal: 5 |
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| operators can handle almost any query! |
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